

$$\star \nabla = \vec{i} \frac{\partial}{\partial x} + \vec{j} \frac{\partial}{\partial y} + \vec{k} \frac{\partial}{\partial z}$$

$$\star \text{Laplacian operator } \nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$$

$$\star \vec{A} \times (\vec{B} \times \vec{C}) = (\vec{A} \cdot \vec{C}) \vec{B} - (\vec{A} \cdot \vec{B}) \vec{C}$$

$$\star [\vec{A} \ \vec{B} \ \vec{C}] = \vec{A} \cdot (\vec{B} \times \vec{C}) = \vec{B} \cdot (\vec{C} \times \vec{A}) = [\vec{B} \ \vec{C} \ \vec{A}] \\ = \vec{C} \cdot (\vec{A} \times \vec{B}) = [\vec{C} \ \vec{A} \ \vec{B}]$$

$$\star \text{Grad } \phi = \overset{=\nabla\phi}{\left(\vec{i} \frac{\partial}{\partial x} + \vec{j} \frac{\partial}{\partial y} + \vec{k} \frac{\partial}{\partial z} \right) \phi} \\ = \vec{i} \frac{\partial \phi}{\partial x} + \vec{j} \frac{\partial \phi}{\partial y} + \vec{k} \frac{\partial \phi}{\partial z} = \sum \vec{i} \frac{\partial \phi}{\partial x}$$

$$\star \text{Div } \vec{F} = \nabla \cdot \vec{F} = \left(\vec{i} \frac{\partial}{\partial x} + \vec{j} \frac{\partial}{\partial y} + \vec{k} \frac{\partial}{\partial z} \right) \cdot \vec{F} \\ = \vec{i} \cdot \frac{\partial \vec{F}}{\partial x} + \vec{j} \cdot \frac{\partial \vec{F}}{\partial y} + \vec{k} \cdot \frac{\partial \vec{F}}{\partial z} \\ = \sum \vec{i} \cdot \frac{\partial \vec{F}}{\partial x}$$

$$\star \text{curl } \vec{F} = \nabla \times \vec{F} = \left(\vec{i} \frac{\partial}{\partial x} + \vec{j} \frac{\partial}{\partial y} + \vec{k} \frac{\partial}{\partial z} \right) \times \vec{F} \\ = \vec{i} \times \frac{\partial \vec{F}}{\partial x} + \vec{j} \times \frac{\partial \vec{F}}{\partial y} + \vec{k} \times \frac{\partial \vec{F}}{\partial z}$$

* Conservative field

A vector function \vec{F} is called conservative field if

$\int_{P_1}^{P_2} \vec{F} \cdot d\vec{s}$ is independent of the path joining P_1 and P_2 .

$$\therefore \boxed{\vec{F} = \nabla \phi}$$

* The necessary and sufficient condition that a field be conservative is that

$$\boxed{\text{curl } \vec{F} = \vec{0}}$$

* If $\text{curl } \vec{F} = \vec{0}$ then F is irrotational.